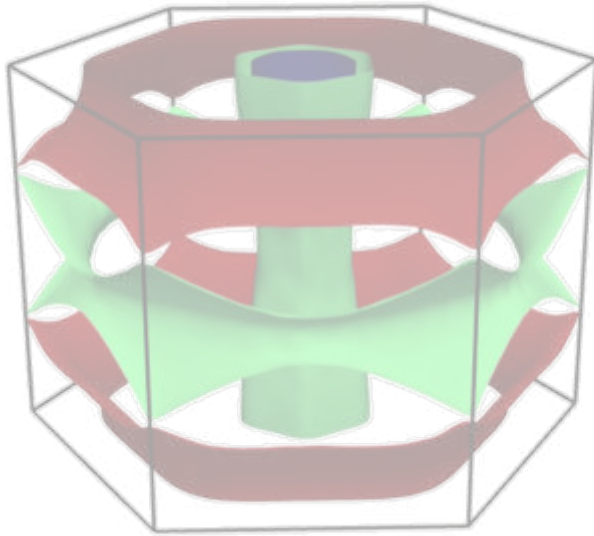




Department of Physics and Astronomy
West Virginia University



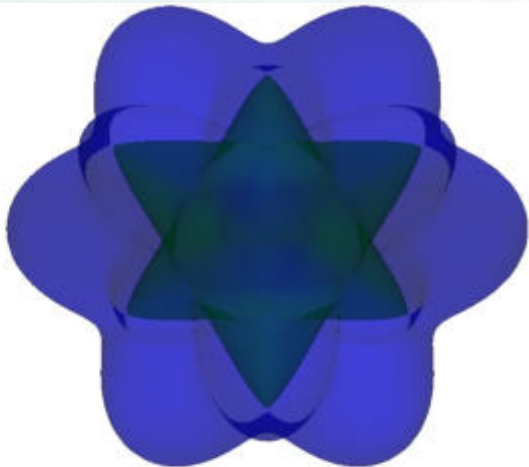
Recent Developments in Pyprocar and MechElastic

Pyprocar Contributors

Uthpala Herath, Pedram Tavadze, Xu He, Eric Bousquet, Sobhit Singh, Reese Boucher, Logan Lang, Freddy Farah, Francisco Muñoz and Aldo H. Romero

MechElastic Contributors

Logan Lang, Sobhit Singh, Viviana Dovale-Farelo, Uthpala Herath, Pedram Tavazohi, François-Xavier Coudert, Aldo H. Romero



Pyprocar



PROCAR lm decomposed
of k-points: 200 # of bands: 48 # of ions: 5

k-point 1 : 0.00000000 0.00000000 0.00000000 weight = 0.00500000

band 1 # energy -29.05690371 # occ. 2.00000000

ion	s	py	pz	px	dxy	dyz	dz2	dxz	x2-y2	tot
1	0.972	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.972
2	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
3	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
4	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
5	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
tot	0.974	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.974

0.000000000	1.203497247	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.7213197256E-01	1.206644141	0.029906	0.000944	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.1442639451	1.215535536	0.014263	0.001967	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.2163959177	1.226439061	0.004364	0.002027	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.2885278902	1.235537941	0.000056	0.001289	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.3606598628	1.233460228	0.002649	0.000051	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.4327918353	1.228146745	0.000000	0.000002	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.5049238079	1.206604221	0.000000	0.000011	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.5770557805	1.195644770	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.6491877530	1.198648720	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.7213197256	1.172068978	0.000000	0.001263	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.7934516981	1.143774531	0.000000	0.000369	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
0.8655836707	1.139814551	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000

k = 0.000000000 0.000000000 0.000000000

==== e(1) = -50.21339 eV ====

psi = 0.478*[# 1]+0.478*[# 14]+0.010*[# 2]+0.010*[# 15]+0.004*[# 28]
+0.004*[# 32]+0.004*[# 36]+0.004*[# 40]+0.002*[# 9]+0.002*[# 22]

|psi|^2 = 1.000

==== e(2) = -50.21339 eV ====

psi = 0.477*[# 1]+0.477*[# 14]+0.009*[# 2]+0.009*[# 15]+0.005*[# 28]
+0.005*[# 32]+0.005*[# 36]+0.005*[# 40]+0.002*[# 9]+0.002*[# 22]

|psi|^2 = 1.000

==== e(3) = -24.41820 eV ====

psi = 0.485*[# 3]+0.485*[# 16]+0.006*[# 6]+0.006*[# 19]+0.002*[# 27]

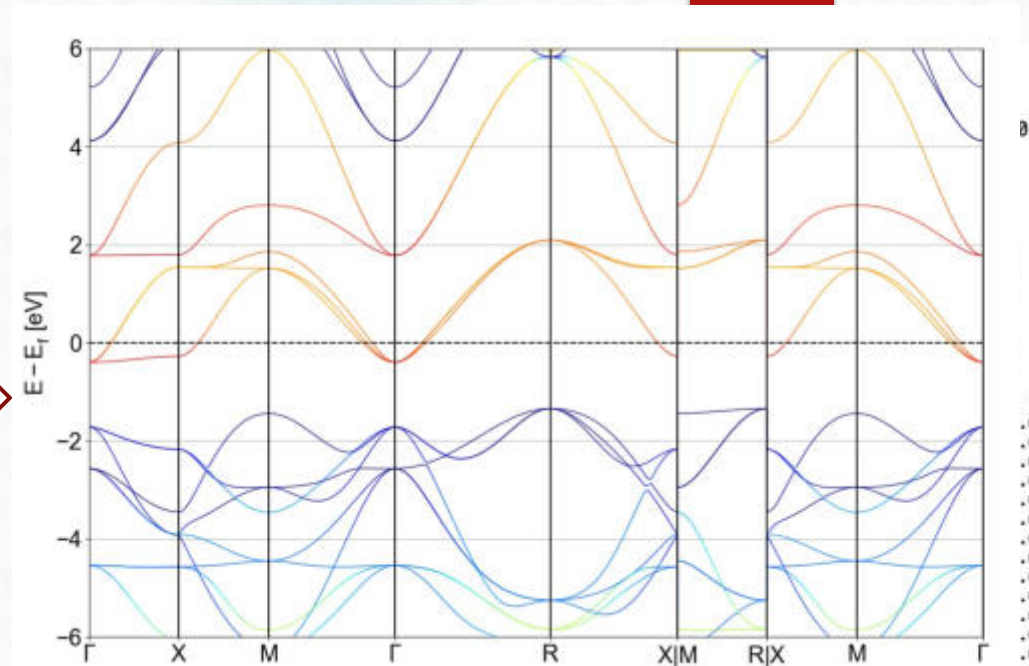
- Simple, single line commands

```
$pyprocar.bandsplot('PROCAR',mode='parametric',
orbitals=[4,5,6],code='vasp'...)
```

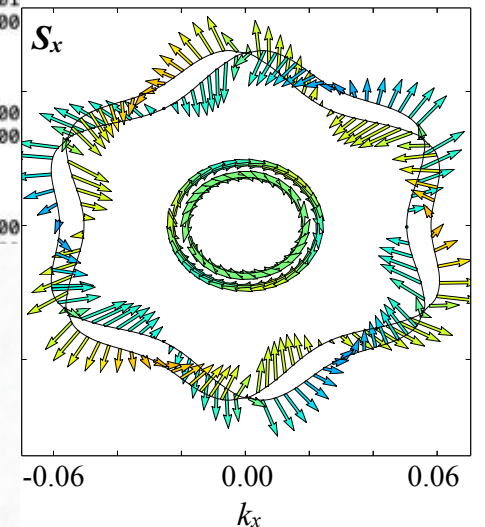
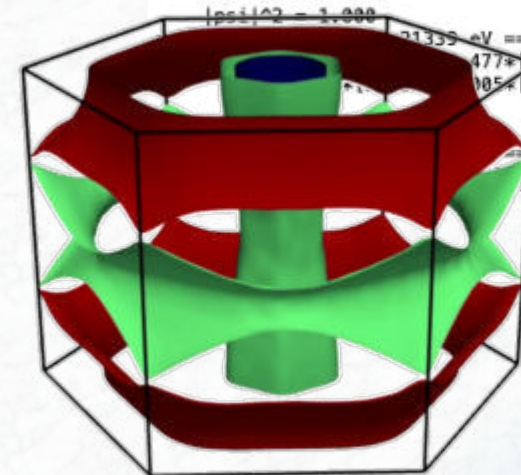
- Supports multiple DFT codes

VASP, Quantum Espresso, Abinit, Elk, Lobster
Siesta*, DFTB+*

Pyprocar



k = 0.0000000000 0.0000000000 0.0000000000
==== e(1) = -50.21339 eV =====
psi = 0.478*[# 1]+0.478*[# 14]+0.01
+0.004*[# 32]+0.004*[# 36]+0.00



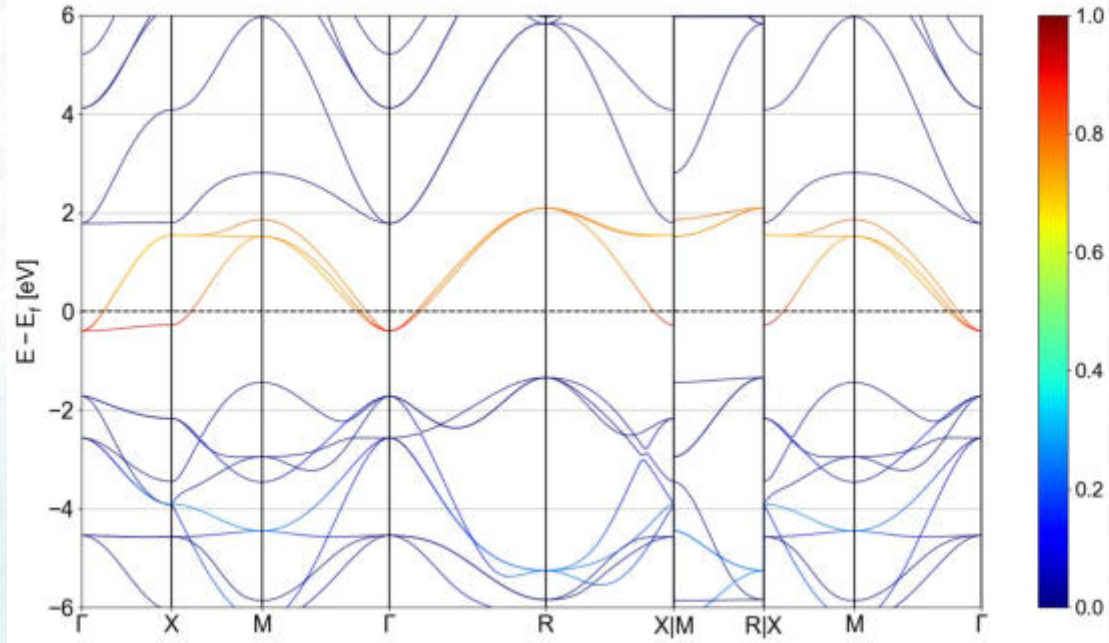
- Simple, single line commands

```
$pyprocar.bandsplot('PROCAR',mode='parametric',  
orbitals=[4,5,6],code='vasp'...)
```

- Supports multiple DFT codes

VASP, Quantum Espresso, Abinit, Elk, Lobster
Siesta*, DFTB+*

Plotting band structures



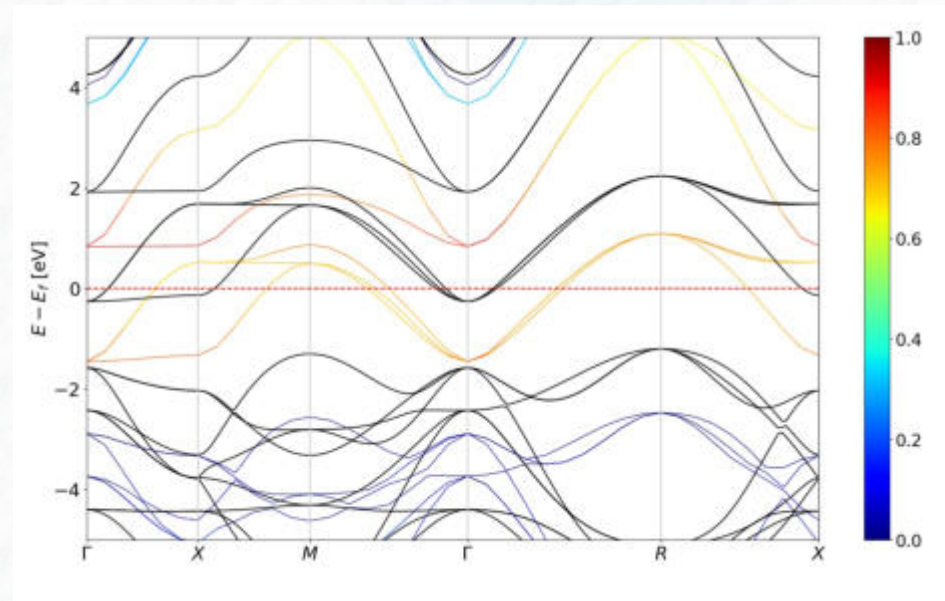
Perform a combination of one or more projections.

$V - d_{t2g}$

```
pyprocar.bandsplot(..., mode='parametric', atoms=[1],  
                    orbitals=[4,5,7])
```

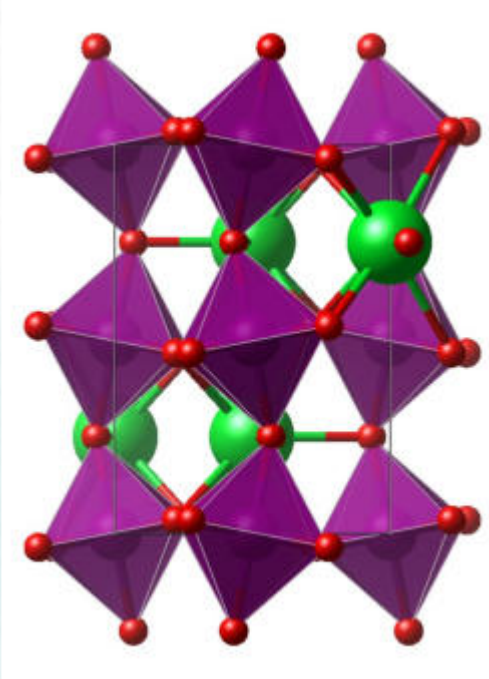
Export plots as matplotlib objects for further processing

```
ax=pyprocar.bandsplot(..., mode='plain', code='elk')  
pyprocar.bandsplot(..., mode='parametric', code='vasp', ax=ax)
```

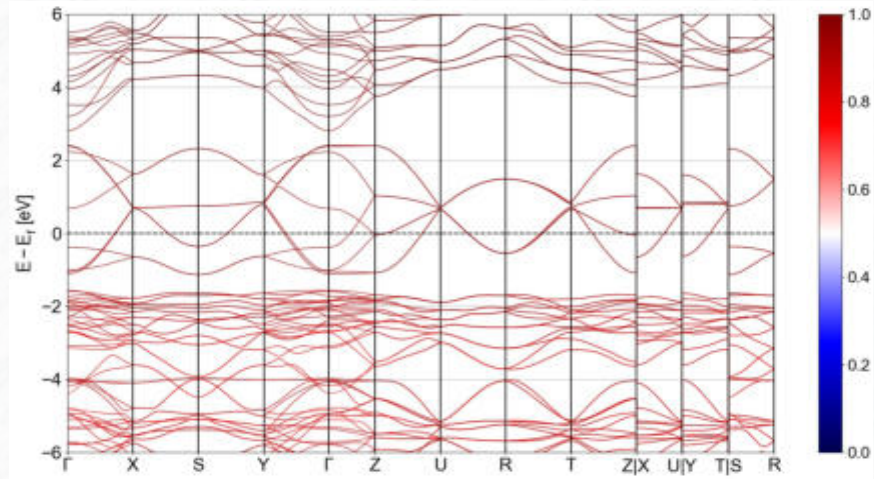


Plotting band structures

Collinear spin calculations

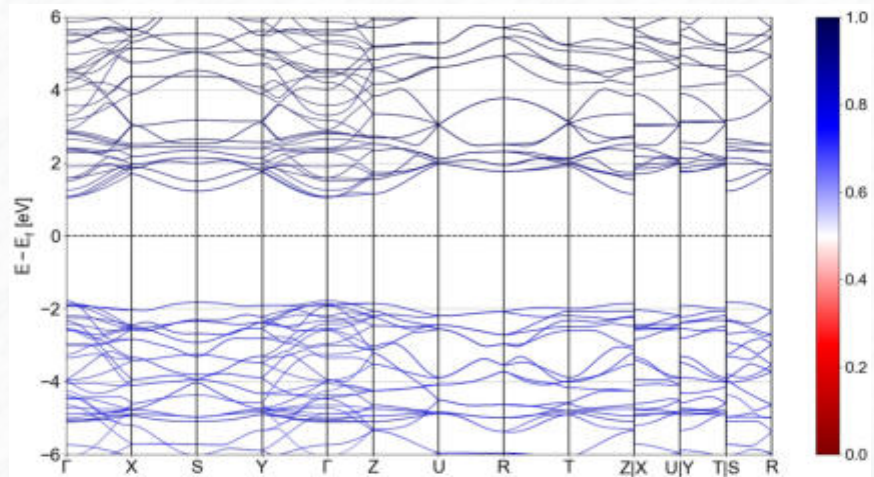


$\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$



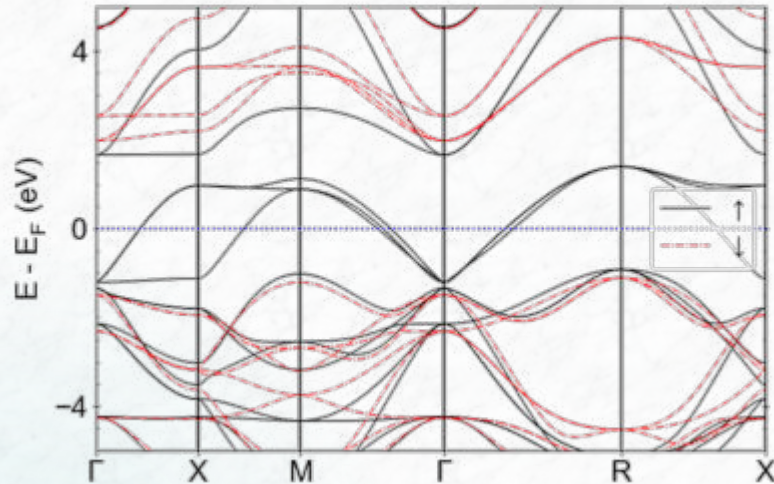
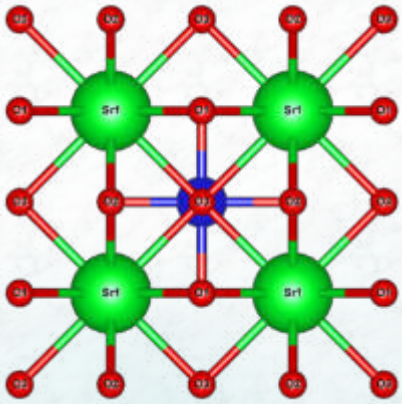
Spin up

```
pyprocar.bandsplot(..., spin=1, separate=True)
```

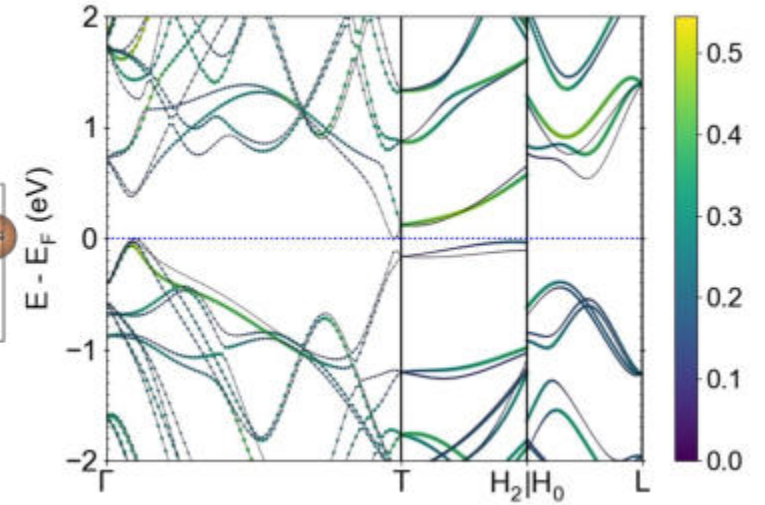
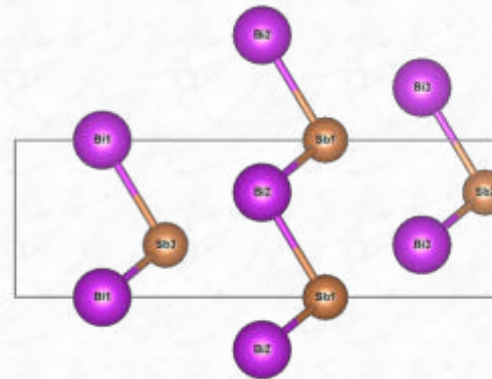


Spin down

Plotting band structures



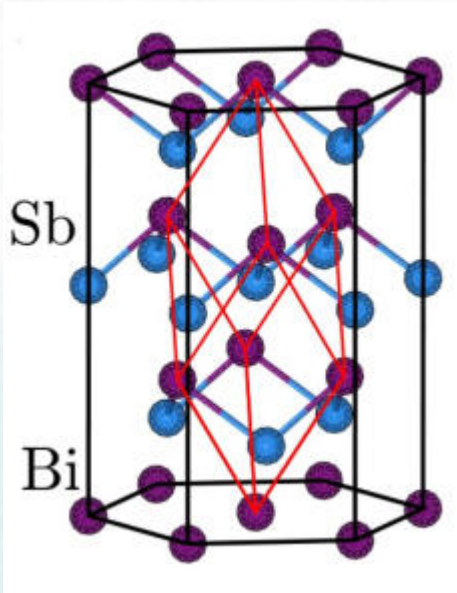
```
pyprocar.bandsplot(mode='plain',
    linestyle=['solid', 'dashdot'],
    colors=["black", "red"],
    elimit=[-5, 5],
    savefig="SrV03-spin-pol.png",
    show=True,
    legend=True,
)
```



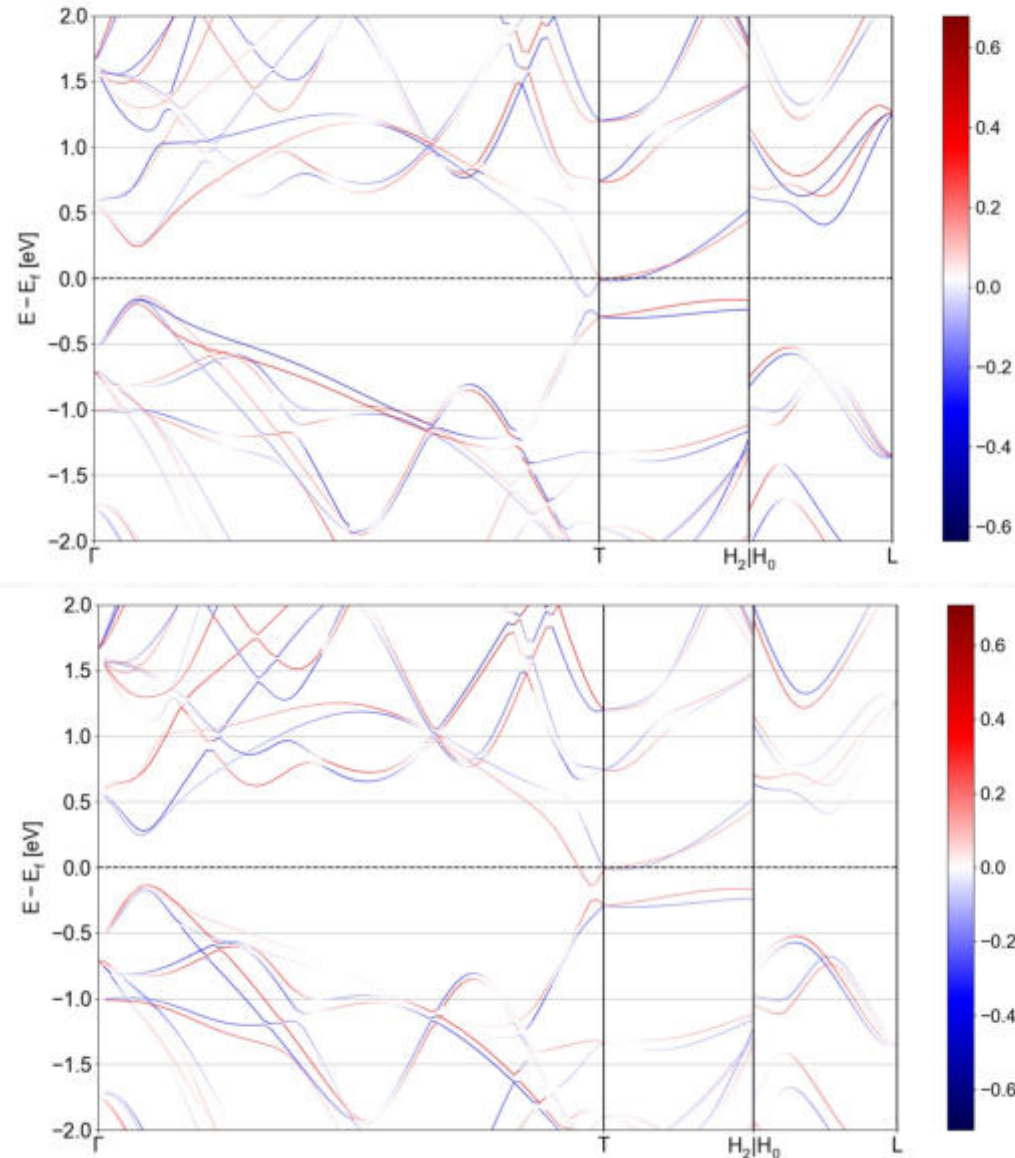
```
ebs_plot = pyprocar.bandsplot(mode='scatter',
    legend=False,
    spins=[0, 1],
    orbitals=['p'],
    atoms=['Bi'],
    weighted_color=True,
    weighted_width=True,
    elimit=[-2, 2]
)
pyprocar.bandsplot(mode='plain',
    legend=False,
    opacities=[0.5],
    elimit=[-2, 2],
    ax=ebs_plot.ax)
```

Plotting band structures

Non-collinear spin calculations



BiSb



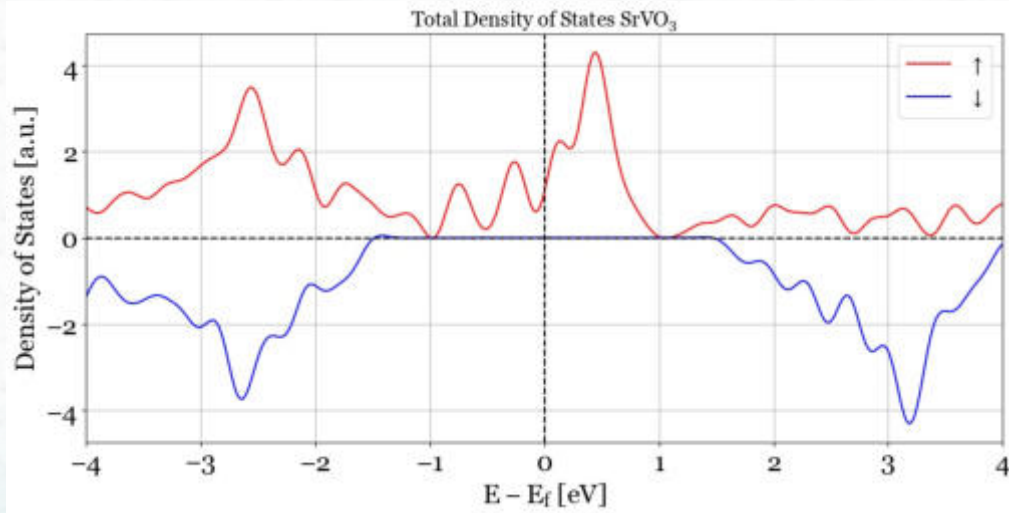
S_x

```
pyprocar.bandsplot(..., spin=1)
```

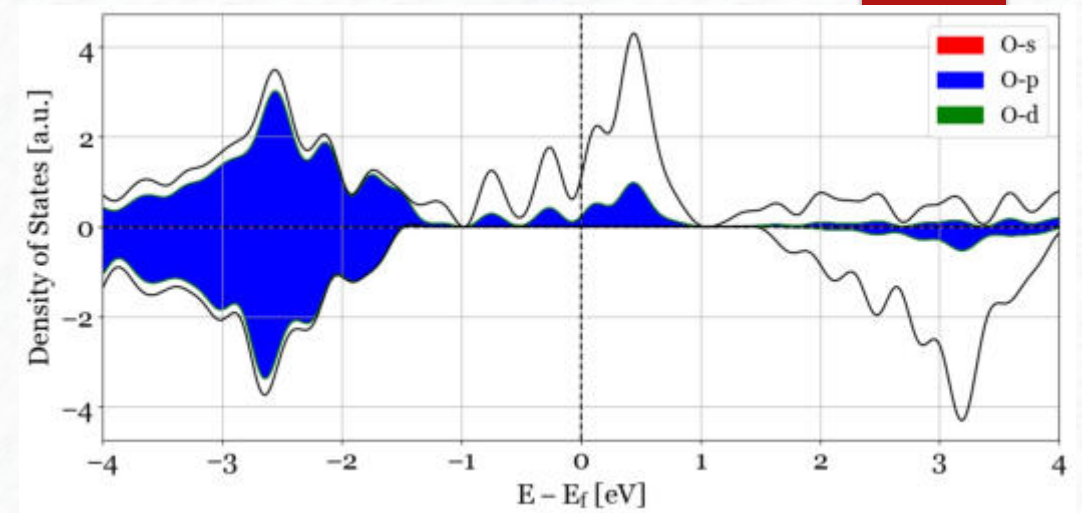
S_y

```
pyprocar.bandsplot(..., spin=2)
```

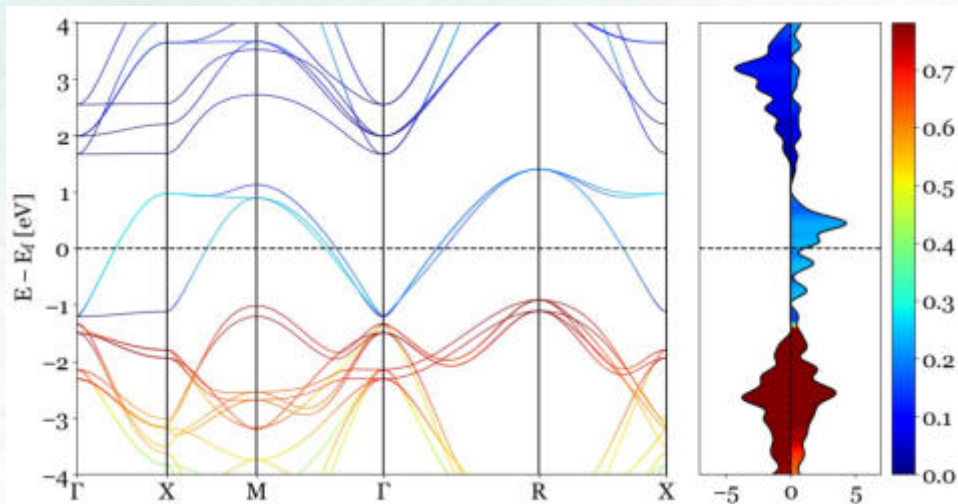
Density of States



```
pyprocar.dosplot(mode='plain')
```



```
pyprocar.dosplot(mode='stack_orbitals')
```



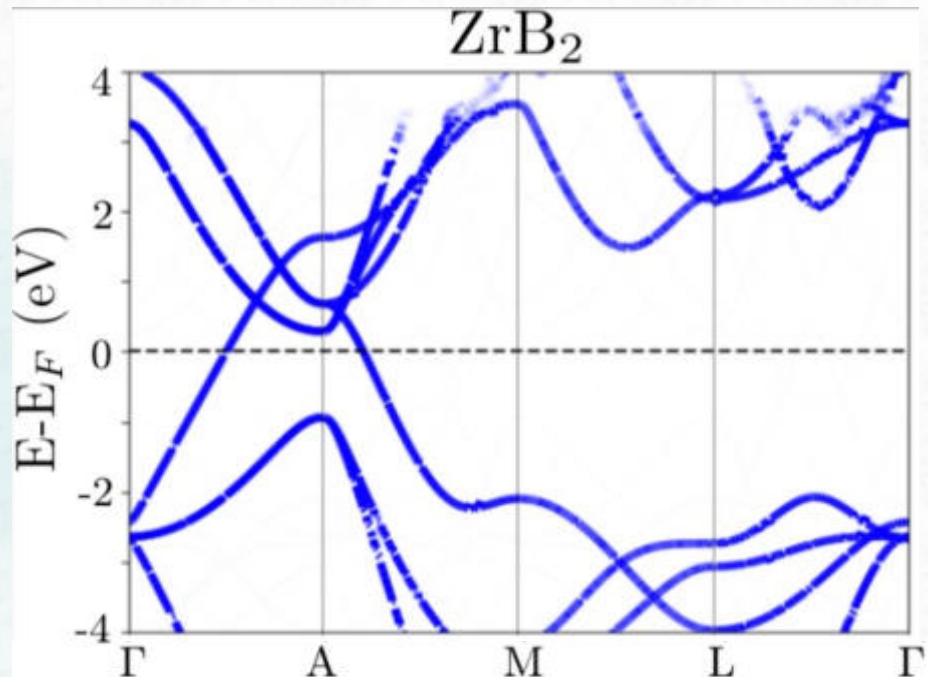
Partial Density of States + Band structure

```
pyprocar.bandsdosplot(vasprunfile='vasprun.xml',  
bands_file='PROCAR',bands_mode='parametric',dos_mode='parametric',  
orbitals=[1,2,3],atoms=[2,3,4],...)
```

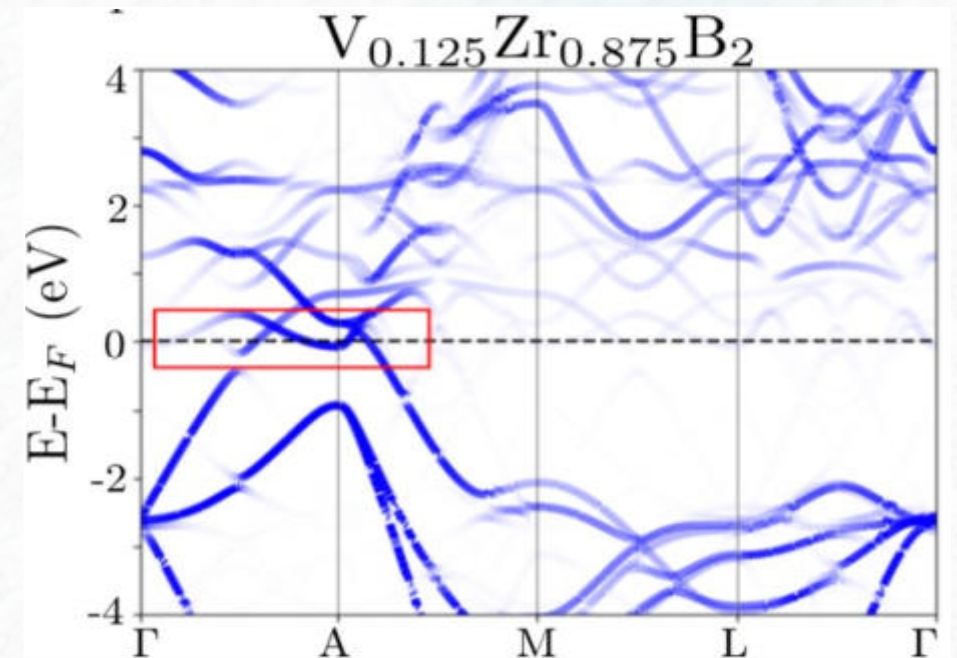
Band unfolding

- Useful to unfold bands from supercells to compare with primitive cell.

E.g. - 10% of V doping can induce superconductivity in ZrB₂. A 2 x 2 x 2 supercell was used to see the changes in the electronic structure.



Primitive cell band structure



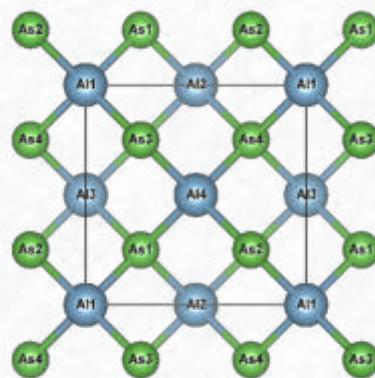
Unfolded band structure of supercell

```
pyprocar.unfold( fname='PROCAR', supercell_matrix=np.diag([2, 2, 2]), ispin=None, show_band=True, width=4, ...)
```



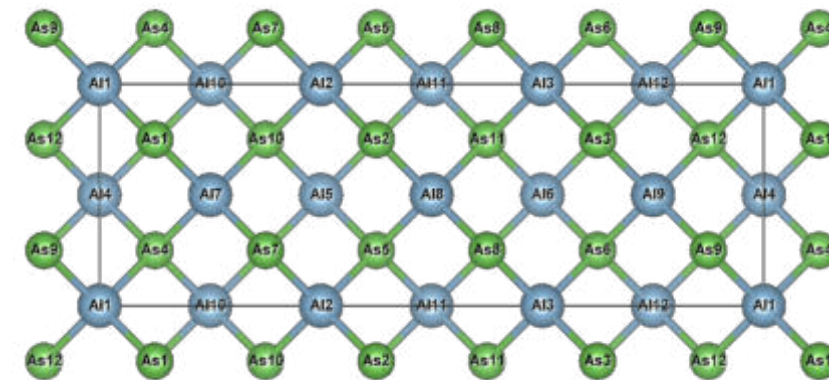
$$\begin{bmatrix} -1, & 1, & 1 \\ 1, & -1, & 1 \\ 1, & 1, & -1 \end{bmatrix}$$

Primitive

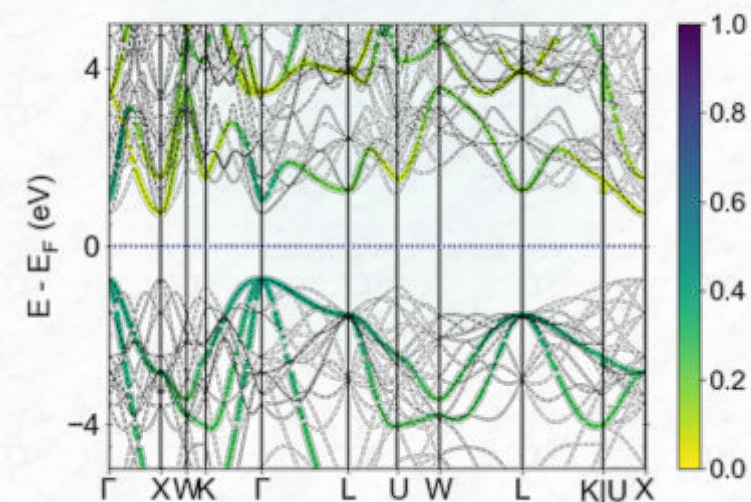
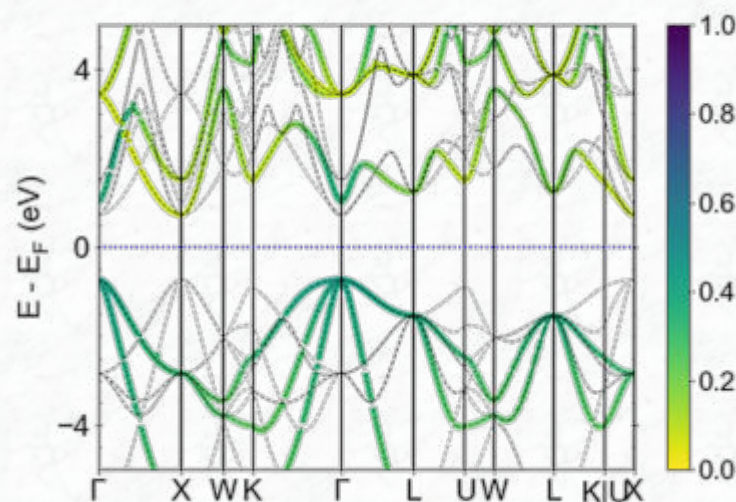
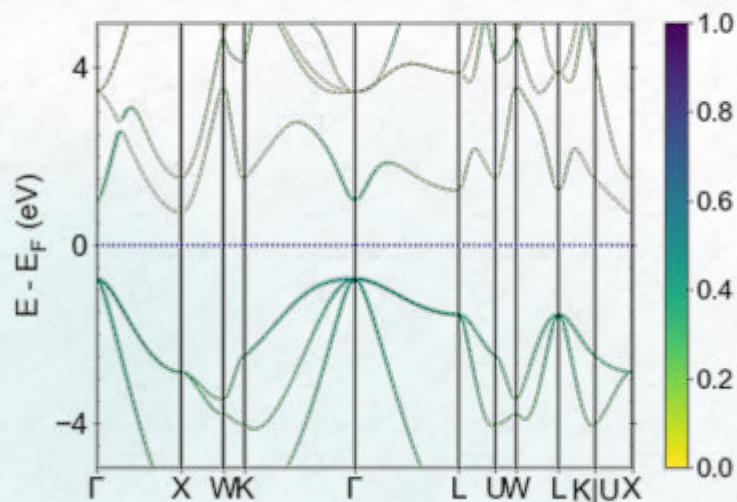


$$\begin{bmatrix} 1, & 0, & 0 \\ 0, & 1, & 0 \\ 0, & 0, & 3 \end{bmatrix}$$

Conventional



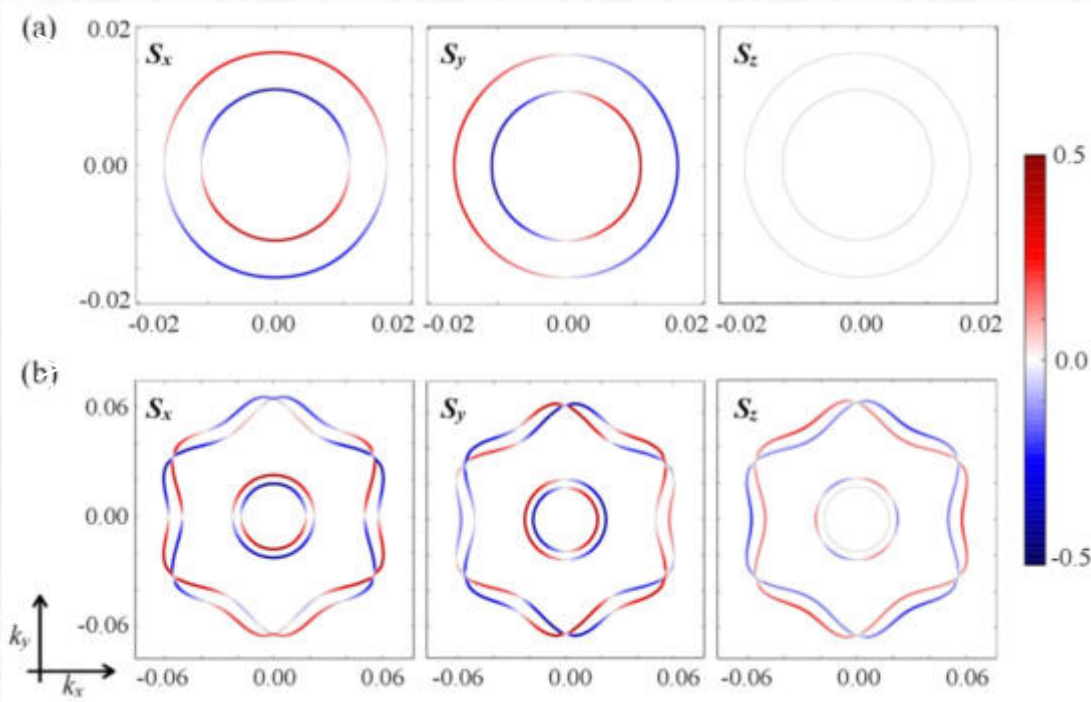
Conventional 1x1x3



```
ebs_plot = pyprocar.bandsplot(procar="PROCAR", poscar="POSCAR", outcar="OUTCAR", kpoints="KPOINTS",
                               mode='parametric',
                               atoms=['As'],
                               unfold_mode=unfolding_mode,
                               transformation_matrix= np.dot(np.diag([1, 1, 3]),M),
                               weighted_width=True,
```

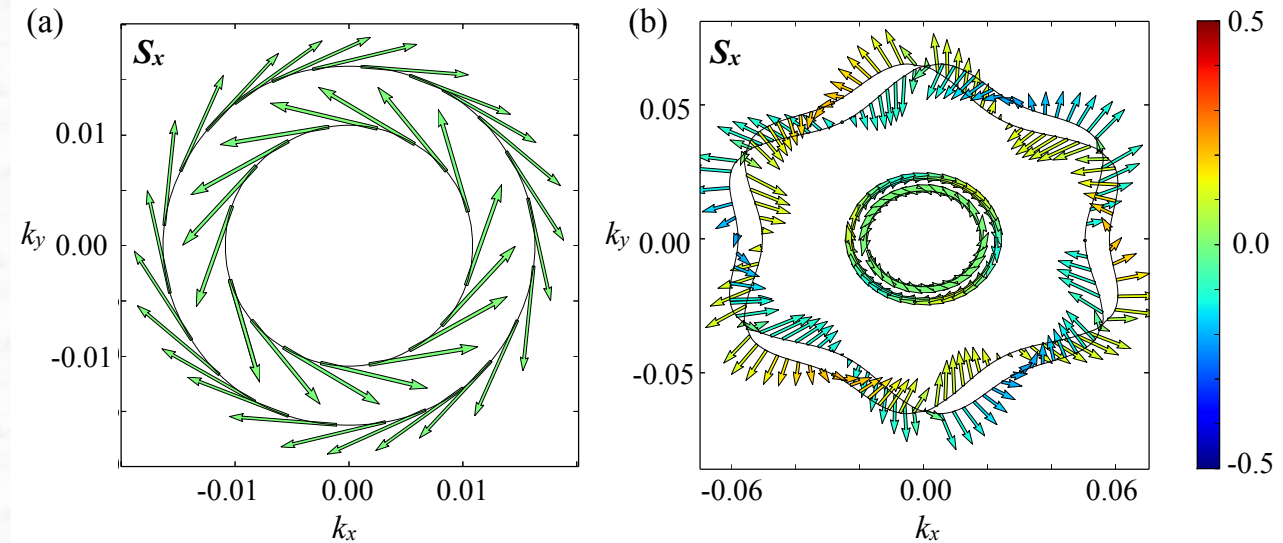
2D spin texture

- Visualize the constant energy surface spin textures in a system.
- Spin texture in BiSb monolayer. Useful to investigate Rashba and Dresselhaus type spin-splitting effects.



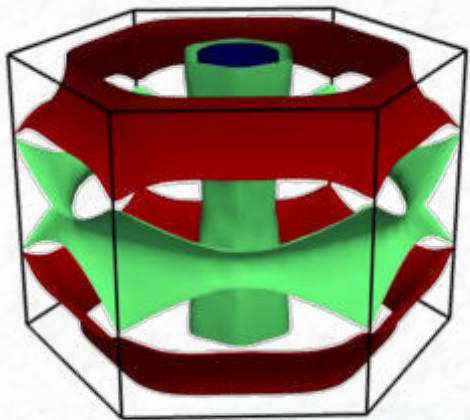
```
pyprocar.fermi2D('PROCAR', st=True, energy=1,  
spin=1, noarrow=True)
```

Representation with arrows

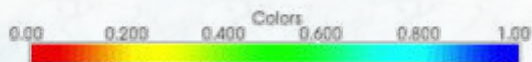


```
pyprocar.fermi2D('PROCAR', st=True, energy=1,  
spin=1, noarrow=False)
```

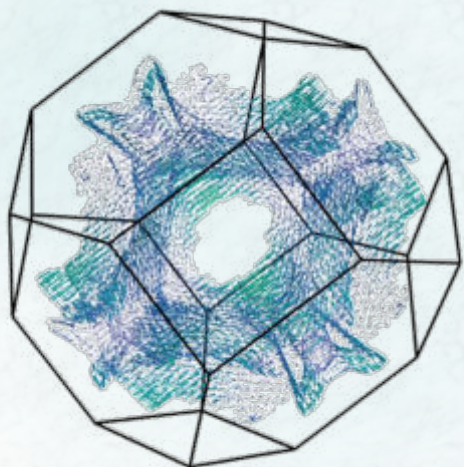
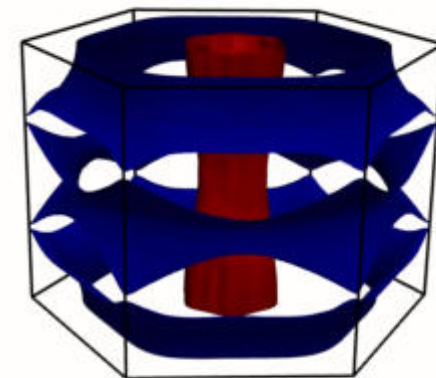
3D Fermi surface



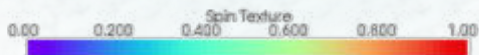
Plain Fermi surface – MgB_2
`pyprocar.fermi3D(mode='plain'...)`



Orbital projected Fermi surface- MgB_2 : B- p_z
`pyprocar.fermi3D(mode='parametric',
orbitals=[3],atoms=[1,2])`

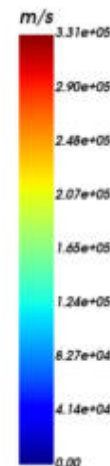
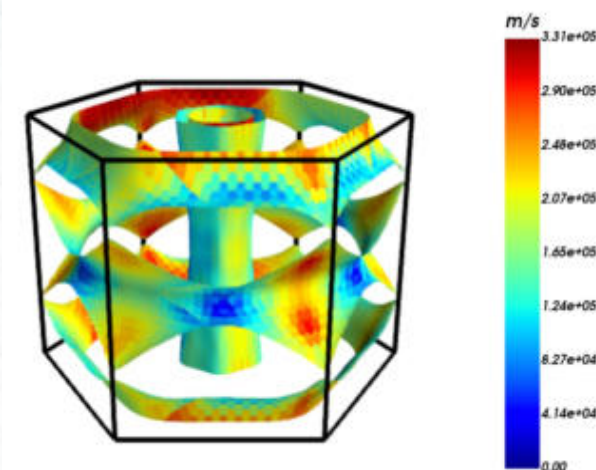


Spin texture surface- BiSb
`pyprocar.fermi3D
(mode='parametric',
spin_texture=True)`



Plotting from external data:
Fermi velocity projection
`pyprocar.fermi3D(mode='external',
color_file='data.dat'...)`

other: effective mass, electron-
phonon coupling



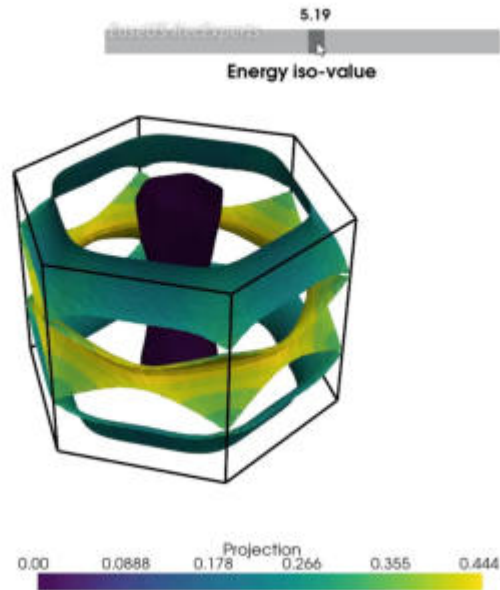
Input formats

- PROCAR format
- bxsf format

Export formats

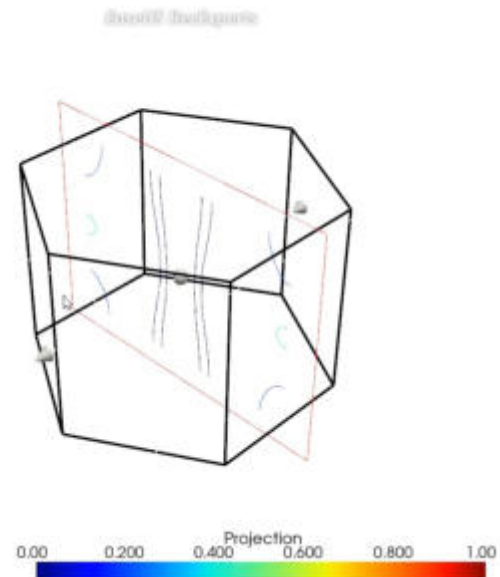
- 2D : png, pdf, ps, ...
- 3D : obj, ply, glb, xml...
- other : gif, mp4

3D Fermi surface



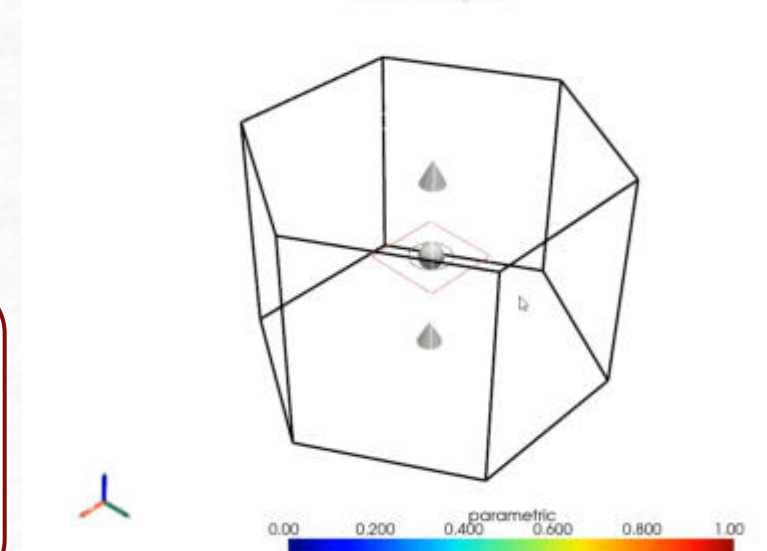
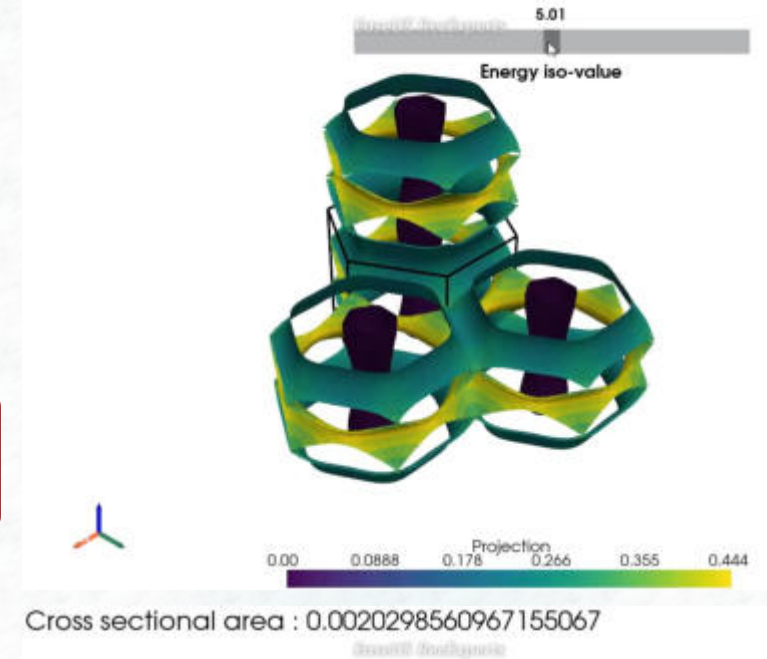
```
pyprocar.fermi3D(...,  
    iso_slider = True,  
    iso_range = 5,  
    iso_surfaces = 5,)
```

```
pyprocar.fermi3D(...,  
    extended_zone_directions=  
    [[1,0,0],[0,1,0],[0,0,1]])
```



```
pyprocar.fermi3D(...,  
    show_slice=True,  
    slice_origin = (0,0,0)  
    slice_normal = (1,0,0))
```

```
pyprocar.fermi3D(...  
    bands = [5],  
    show_slice=True,  
    slice_normal = (0,0,1),  
    slice_origin = (0,0,0),  
    show_cross_section_area= True)
```



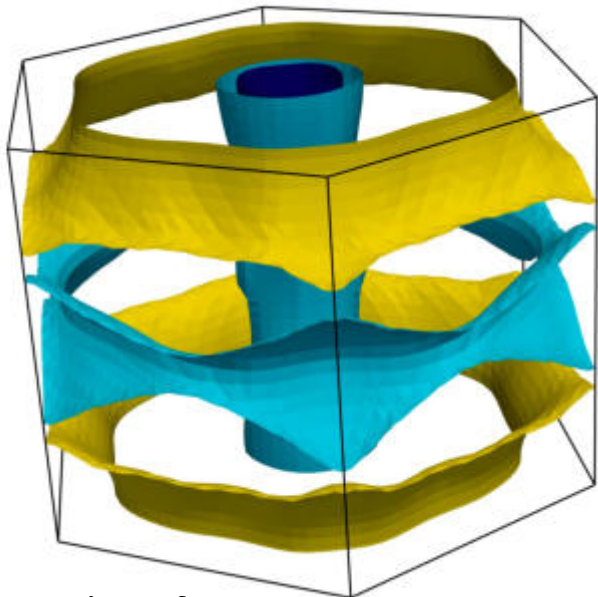
Fermi Surface - Abinit

With Abinit v9+ PROCAR is generated when prtprocar is set in the .in file.

However, due to parallelization, the PROCAR is split into multiple files. To fix this:

Pyprocar.cat(mergeparallel=True, code="abinit") in the directory where the PROCAR_ files are. In a future release this step will be automated.

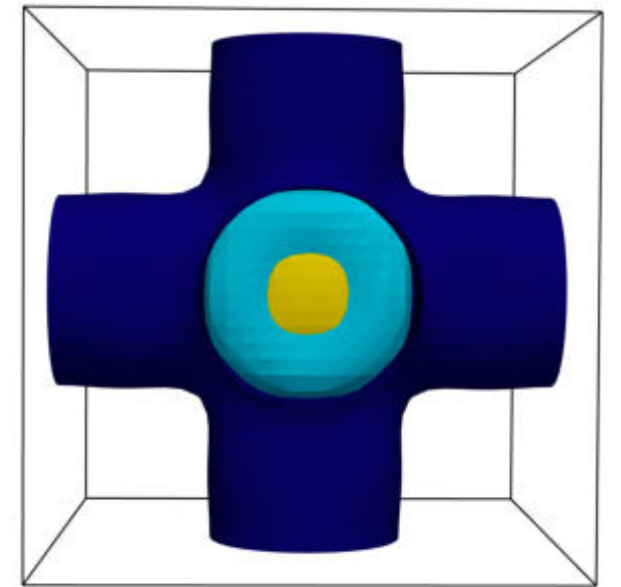
```
pyprocar.fermi3D(  
    "PROCAR",  
    abinit_output="abinit.out",  
    code="abinit",  
    mode="plain",  
    interpolation_factor=4,
```



MgB2 Fermi surface

Another option:

Subtract Fermi surface of different spin polarizations



SrVO3 Fermi surface

MechElastic



- Simple, single line commands

```
mechelastic.calculate_elastic(code="vasp",  
                               dim="3D",  
                               infile="OUTCAR-Si_bulk")
```

- Supports multiple DFT codes

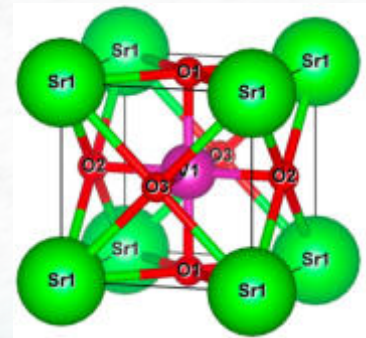
VASP, Quantum Espresso, Abinit,

- Elastic constants and EOS

```
.....  
Elastic Tensor (GPa units)  
.....  
153.138  56.794  56.794  0.000  0.000  0.000  
56.794 153.138  56.794  0.000  0.000  0.000  
56.794  56.794 153.138  0.000  0.000  0.000  
0.000  0.000  0.000 74.717  0.000  0.000  
0.000  0.000  0.000  0.000 74.717  0.000  
0.000  0.000  0.000  0.000  0.000 74.717  
.....  
This matrix was computed from vasp  
Note: For VASP users THIS is the pressure-connected matrix  
.....  
Elastic Tensor Eigen Values (GPa units)  
.....  
[96.138, 266.718, 96.138, 74.717, 74.717, 74.717]  
.....  
Mechanical Stability Tests  
.....  
WARNING: crystal symmetry class was not provided by user, it will be taken from the OUTCAR  
One of the following was expected as the second argument:  
'cubic', 'hexagonal', 'tetragonal', 'rhombohedral-1', 'rhombohedral-2', 'orthorhombic', 'monoclinic'  
From OUTCAR the crystal type is = 'cubic'  
Cubic crystal system  
.....  
Here stability criteria for the stability of cubic system are: Ref.[1]  
(i) C11 - C12 > 0; (ii) C11 + 2C12 > 0; (iii) C44 > 0  
Condition (i) satisfied.  
Condition (ii) satisfied.  
Condition (iii) satisfied.
```

```
.....  
Elastic Moduli  
.....  
Voigt Reuss Average  
Bulk modulus (GPa) 88.906 88.906 88.906  
Shear modulus (GPa) 64.098 61.220 62.659  
Young's modulus (GPa) 155.035 149.374 152.204  
Poisson's ratio 0.209 0.220 0.215  
B-wave modulus (GPa) 174.369 170.532 172.451  
Bulk/Shear ratio 1.387 1.452 1.419 (brittle)  
.....  
Elastic parameters  
.....  
Lame's first and second parameter; Ref.[3]  
Lambda (GPa) = 47.138  
Mu (GPa) = 62.652  
.....  
Bonding information  
.....  
Kleinman's parameter; Ref.[4,5]  
NOTE: K = 0 (1) bending (stretching) would dominate  
K = 0.63391  
.....  
Cauchy's Pressure calculated from the relation : CP = C_12 - C_44  
CP > 0 (+ve) indicates that ionic bonding dominates  
CP < 0 (-ve) indicates that covalent bonding dominates  
CP (GPa) = -17.923  
Bonding is mainly covalent  
.....  
Elastic Anisotropy  
.....  
Zener's anisotropy (true for cubic crystals only); Az = 1.551; Ref.[6]  
Chung-Buessem's anisotropy (true for cubic crystals only); Ach = 0.023; Ref.[7]  
Universal anisotropy index; Au = 0.235; Ref.[8]  
log-Euclidean's anisotropy; Al = 0.103; Ref.[9]
```

MechElastic



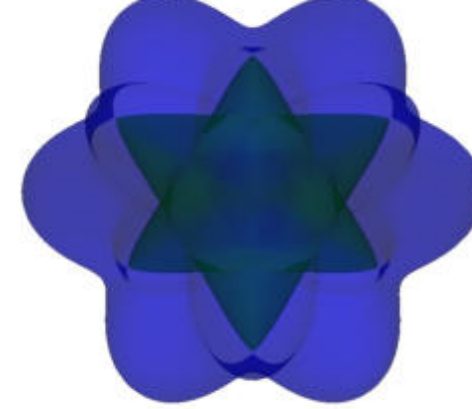
DFT



Quantum Espresso



Numerical data

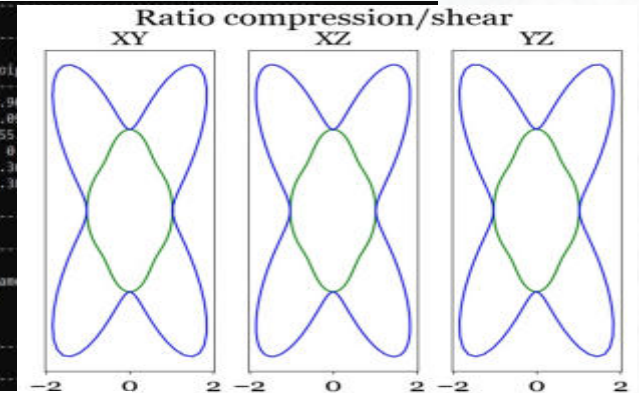


```
Condition (iii) satisfied.

Elastic Moduli
-----
Bulk modulus (GPa) 88.9
Shear modulus (GPa) 64.8
Young's modulus (GPa) 155
Poisson's ratio 0
P-wave modulus (GPa) 174.3
Bulk/Shear ratio 1.3

Elastic parameters
-----
Lame's first and second param
Lambda (GPa) = 47.138
mu (GPa) = 62.652

Bonding information
-----
```



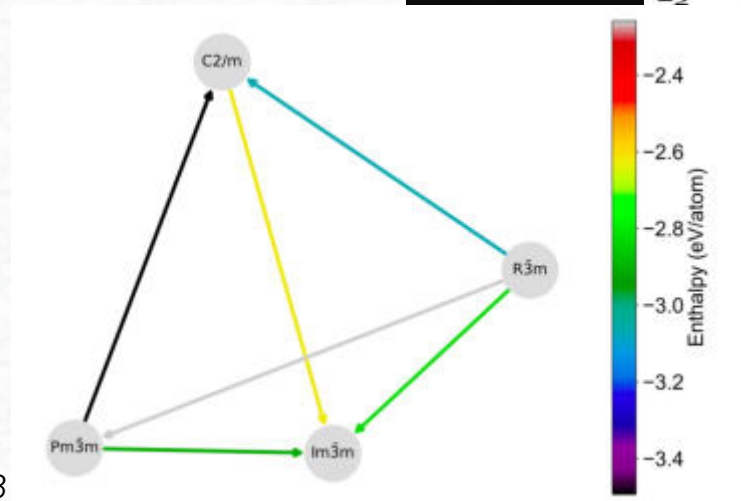
- Simple, single line commands

```
mechelasic.calculate_elastic(code="vasp",  
                             dim="3D",  
                             infile="OUTCAR-Si_bulk")
```

- Supports multiple DFT codes

VASP, Quantum Espresso, Abinit,

- Elastic constants and EOS



```
dominate
can : CP = C_12 - C_44
ing dominates
nding dominates
.....
only); At = 1.551; Ref.[6]
crystals only); Ach = 0.023; Ref.[7]
[0]
[0]
```

MechElastic 3D Analysis

```
mechelastic.calculate_elastic(code="vasp",  
                               dim="3D",  
                               infile="OUTCAR-Si_bulk")
```

Elastic Tensor (GPa units)

153.130	56.794	56.794	0.000	0.000	-0.000
56.794	153.130	56.794	-0.000	-0.000	-0.000
56.794	56.794	153.130	-0.000	0.000	0.000
0.000	-0.000	-0.000	74.717	-0.000	0.000
0.000	-0.000	0.000	-0.000	74.717	0.000
-0.000	-0.000	0.000	0.000	0.000	74.717

This matrix was computed from vasp

Note: For VASP users this is the pressure-corrected matrix

Elastic Tensor Eigen Values (GPa units)

[96.335, 266.718, 96.335, 74.717, 74.717, 74.717]

Mechanical Stability Tests

WARNING: crystal symmetry class was not provided by user, it will be taken from the OUTCAR

One of the following was expected as the second argument:

'cubic', 'hexagonal', 'tetragonal', 'rhombohedral-1', 'rhombohedral-2', 'orthorhombic', 'monoclinic'

From OUTCAR the crystal type is = cubic

Cubic crystal system

Born stability criteria for the stability of cubic system are: Ref.[1]

(i) $C_{11} - C_{12} > 0$; (ii) $C_{11} + 2C_{12} > 0$; (iii) $C_{44} > 0$

Condition (i) satisfied.

Condition (ii) satisfied.

Condition (iii) satisfied.

MechElastic 3D Analysis

Elastic Moduli

	Voigt	Reuss	Average
Bulk modulus (GPa)	88.906	88.906	88.906
Shear modulus (GPa)	64.098	61.220	62.659
Young's modulus (GPa)	155.035	149.374	152.204
Poisson's ratio	0.209	0.220	0.215
P-wave modulus (GPa)	174.369	170.532	172.451
Bulk/Shear ratio	1.387	1.452	1.419 (brittle)

Elastic parameters

Lame's first and second parameter; Ref.[3]

Lambda (GPa) = 47.138

Mu (GPa) = 62.652

Bonding information

Kleinman's parameter; Ref.[4,5]

NOTE: $K = 0$ (1) bending (stretching) would dominate

$K = 0.63391$

Cauchy's Pressure calculated from the relation : $CP = C_{12} - C_{44}$

$CP > 0$ (+ve) indicates that ionic bonding dominates

$CP < 0$ (-ve) indicates that covalent bonding dominates

CP (GPa) = -17.923

Bonding is mainly covalent

Elastic Anisotropy

Zener's anisotropy (true for cubic crystals only); $A_z = 1.551$; Ref.[6]

Chung-Buessem's anisotropy (true for cubic crystals only); $A_{cb} = 0.023$; Ref.[7]

Universal anisotropy index; $A_u = 0.235$; Ref.[8]

Log-Euclidean's anisotropy; $A_L = 0.103$; Ref.[9]

Elastic Wave Velocities and Debye Temperature

Longitudinal wave velocity (v_l) : 8694.638 m/s; Ref.[10]

Transverse wave velocity (v_t) : 5240.943 m/s; Ref.[10]

Average wave velocity (v_m) : 5795.129 m/s; Ref.[10]

Debye temperature : 630.982 K; Ref.[10]

WARNING: The Debye model for the atomic displacement is based on a monoatomic crystal approximation. Here we consider an averaged mass, in case your crystal has several species.

Melting Temperature

Melting temperature calculated from the empirical relation: $T_m = 607 + 9.3 \cdot K_{vrh} \cdot \rho_m^{1/3}$ (in K); Ref.[11]

$T_m = 1433.825$ K (plus-minus 555 K)

WARNING: This is a crude approximation and its validity needs to be checked!

Hardness Analysis

Hardness (H_{1a}) = 9.24 GPa; Ref.[12]

Hardness (H_{1b}) = 9.24 GPa; Ref.[12]

Hardness (H_2) = 8.19 GPa; Ref.[13]

Hardness (H_3) = 9.66 GPa; Ref.[14]

Hardness (H_4) = 6.96 GPa; Ref.[15]

Hardness (H_5) = 11.94 GPa; Ref.[16]

Hardness recommendation model:

	Cubic	Hexagonal	Orthorhombic	Rhombohedral	General
Insulator	H2	H1b	H2	H2	H2
Semiconductor	H5	H1b, H3		H2	H5
Metal	H1a	H4	H4	H4	H4
Insulator	: bandgap > 2 eV				
Semiconductor	: bandgap < 2 eV				
Metal	: bandgap = 0				

The MechElastic 2D Analysis

```
import mechelastic
mechelastic.calculate_elastic(code="vasp",
                              dim="2D",
                              infile="OUTCAR-graphene",
                              lattice_type = 'hexagonal')
```

Elastic tensor for two-dimensional system in N/m units

334.1501	89.8781	0.8525	-0.0015	-0.0169	0.0009
89.8781	334.2872	0.8606	0.0018	0.0115	0.0013
0.8525	0.8606	-0.7386	0.0170	-0.0437	-0.0004
-0.0015	0.0018	0.0170	-1.6537	0.0009	-0.0073
-0.0169	0.0115	-0.0437	0.0009	-0.4477	-0.0042
0.0009	0.0013	-0.0004	-0.0073	-0.0042	122.0850

Mechanical Stability Test

Hexagonal lattice

Stability criteria for the stability of hexagonal system are:

(i) $C_{11} + C_{12} > 0$; (ii) $C_{11} - C_{12} > 0$;

Condition (i) satisfied.

Condition (ii) satisfied.

Elastic properties in two-dimensions

[Useful refs. Andrew et al.; Phys. Rev. B 85, 125428 (2012), Peng et al., Acta Mechanica 223 (2012), 2591-2596; Comput. Mater. Sci. 68, 320 (2013); Mech. Mater. 64, 135 (2013)]

```
-----
2D layer modulus (N/m)      :      212.048
2D Young's modulus Y[10] (N/m) :      309.985
2D Young's modulus Y[01] (N/m) :      310.112
2D Shear modulus G (N/m)    :      122.085
2D Poisson ratio v[10]      :          0.269
2D Poisson ratio v[01]      :          0.269
-----
```

EOS module

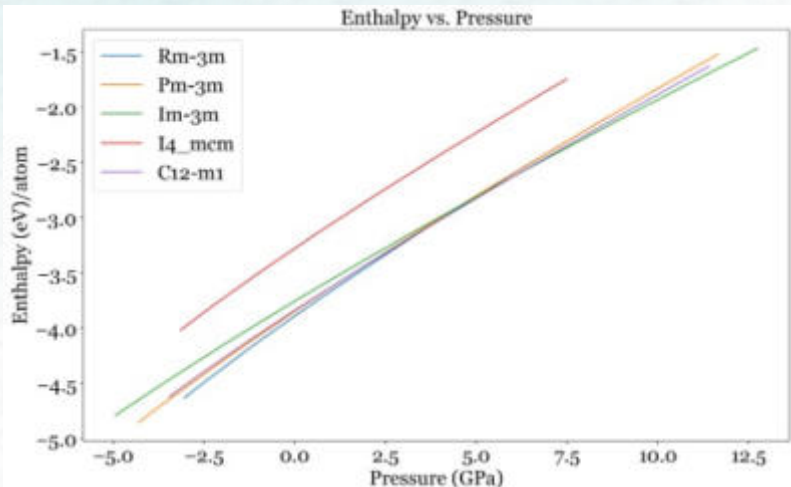
Enthalpy Curves

$$H=U+PV$$

```
eos_object = EOS()
```

```
infiles = ["Rm-3m", "Pm-3m",  
          "Im-3m", "I4_mcm",  
          "C12-m1"]
```

```
natoms = [6, 1, 2, 9, 4]  
eos_object.plot_enthalpy_curves(infiles,  
                                eostype = 'energy', natoms, au=False)
```

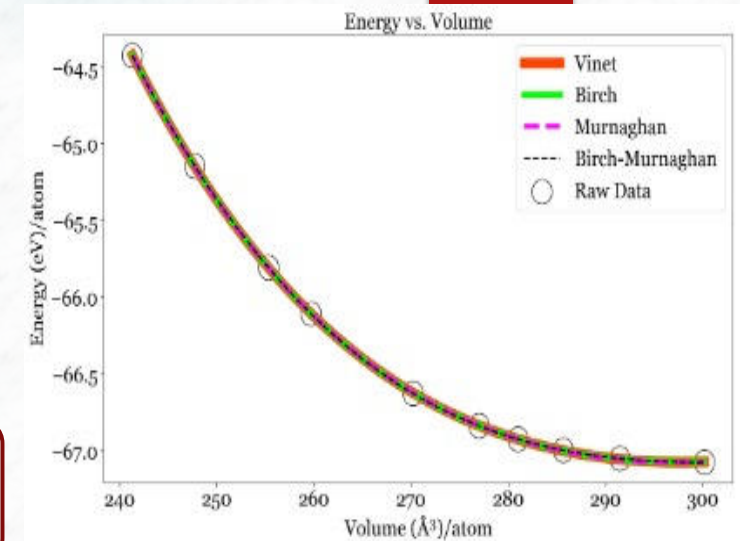


EvsV.dat

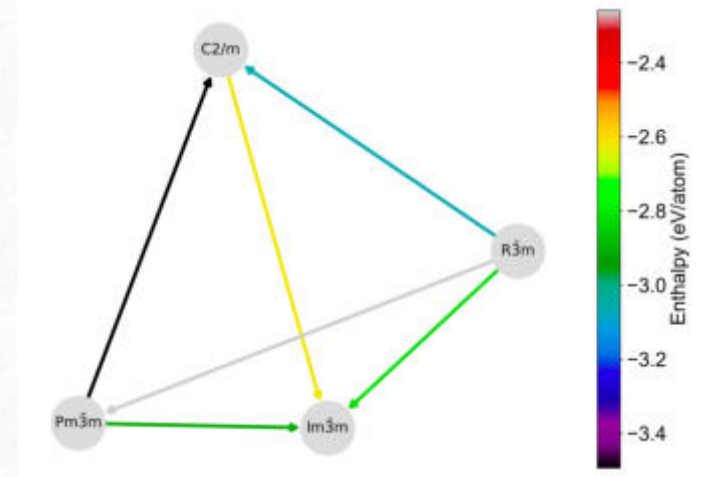
```
300.21 -67.07549985  
291.50 -67.05105419  
285.67 -66.99700837  
281.02 -66.92530138  
277.00 -66.83788211  
270.22 -66.62790736  
259.71 -66.10926114  
255.34 -65.80844965  
247.75 -65.14777164  
241.31 -64.42659671
```

```
eos = EOS("EvsV.dat")  
eos.plot_eos(au=False)
```

Curve Fitting

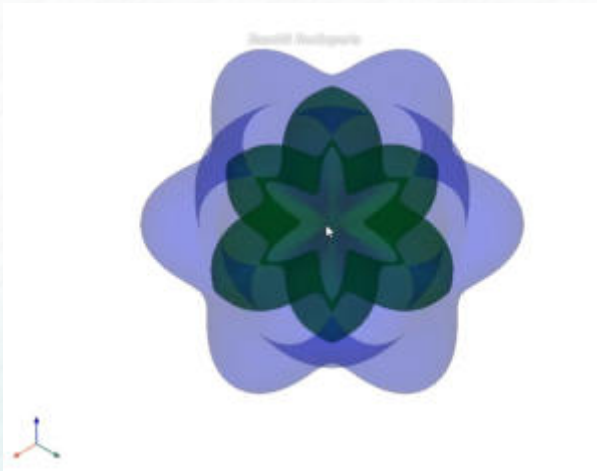
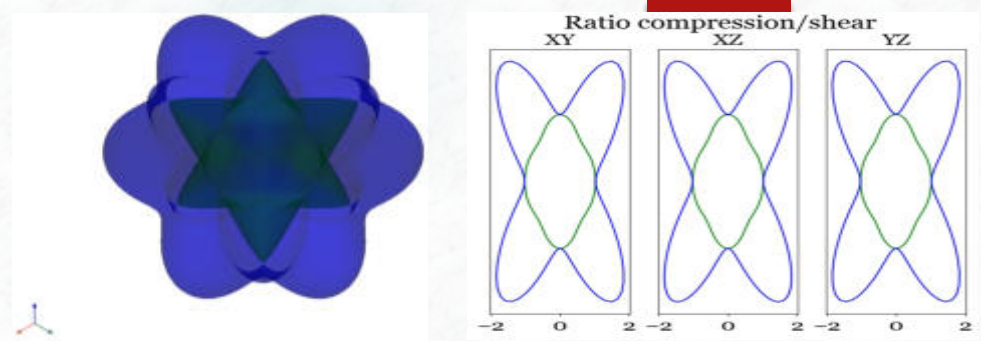


Phase transition paths



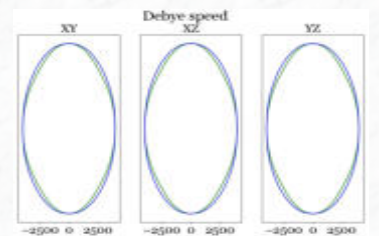
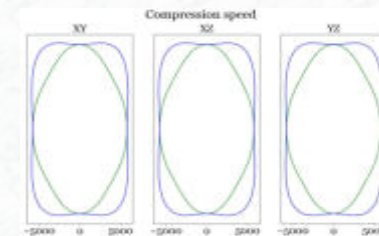
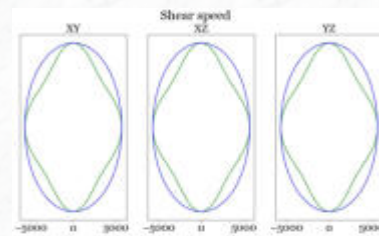
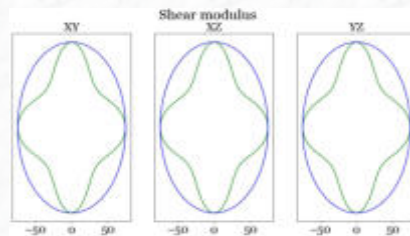
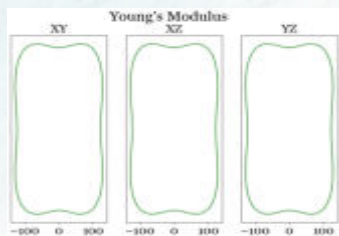
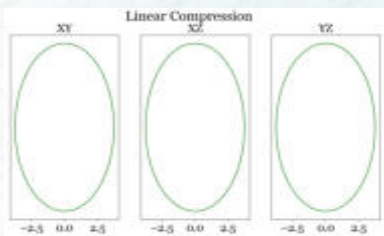
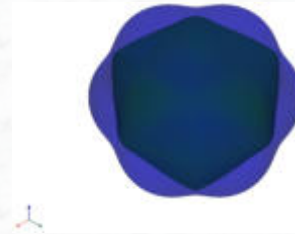
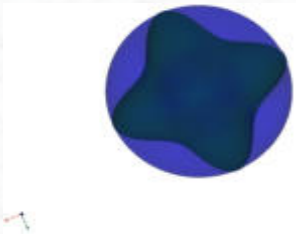
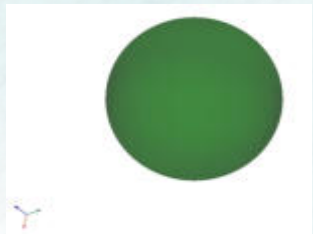
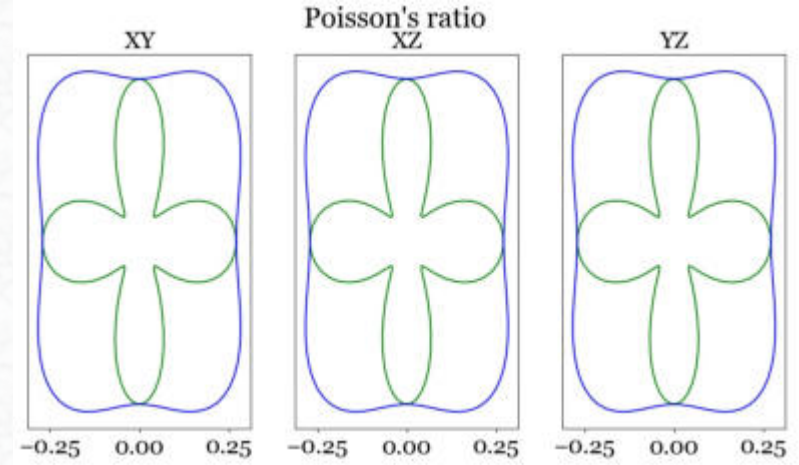
A network plot of the phase transition paths for different phases of Bi. The color of the arrows represents the relative enthalpy for different phase transitions.

2D and 3D Visualizations of Elastic Properties



```
Output1,meshes= mechelastic.calculate_elastic(...,  
plot= "3D"  
elastic_calc= "POISSON"  
show = True)
```

```
Output2,fig = mechelastic.calculate_elastic(... ,  
plot= "2D"  
elastic_calc= "POISSON"  
show=True )
```



Perspectives

Development of two packages to perform electronic structure and elastic analysis of electronic structure calculations.

Perspectives:

- Improve the Fermi surface topology.

- Correlate Fermi area cross section with the De Haas-van Alphen Effect (Verstraete).

- Compute the Gyrotropic Magnetic Effect (we need extra terms, Fermi curvature).

- Extend the package to perform Wavefunction or density analysis.

- Some ideas from the community are also considered.